

## Probability \& Bridge

## NKy Summer Getaway Sectional

## August 12, 2017

## Goals

- Practical bridge advice
- Improve how we think at the table
- Get better results in tough contracts
- NOT: combinatorial mathematics or statistical equations.


$$
\binom{N}{n}=\frac{N!}{n!(N-n)!}
$$

# Simple Chances 

- Flip a coin
- Roll a die
- Take a finesse


## Flip a Coin

- Coin has two sides (2 Total cases)
- One side is up (1 Specific Case): Heads or Tails
- a priori probability $=$ specific $/$ TOTA $=1 / 2=50 \%$
- Each coin toss is INDEPENDENT of the prior event (Coins have no memories)
- Probability of success for both of 2 independent events is the product of the probability of each:
- Two coins giving heads (HH): $1 / 2 \times 1 / 2=25 \%$
-3 Coins giving Heads (HHH): $25 \%$ X $1 / 2=12.5 \%$ etc...


## Coin Quiz

- Which sequence of 10 coin tosses is more likely?

Sequence A: HHHHHHHHHH 0.0977\% Sequence B: THTTHTHHHT 0.0977\%

## Rolling a Die

- A standard die has 6 sides -6 Total cases
- One side shows up - 1 Specific Case.
- The roll of any one die each number has an equal probability of $1 / 6=16.67 \%$
- Each role is INDEPENDENT (die has no memory)
- Q: With two fair dice, what is the probability of rolling a 7 ?


## Rolling a 7

－Outcome table（6x6＝36 Total Cases）$\rightarrow$
－Frequency Table：

| $\cdot \cdot$ | $\cdot$ | $\cdot$ | $\cdot$ | －$\because$ | － |
| :---: | :---: | :---: | :---: | :---: | :---: |
| －$\cdot$ | Q． | $\square$ | － 0 | $\square$ | ［1］ |
| $\odot$ | $\odot$ | $\odot$ | $\bullet$ | $\odot$ | 8 |
| 88 | 88. | $8 \cdot 8$ | 18： | $18 \%$ | 8 |
| 88 | $8 \cdot 8$ | 88 | $88:$ | 888 | 8. |
| 19， | 田 | 目 | 成： | 目 | 1 |


| $\#$ | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | Tot |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Cases | 1 | 2 | 3 | 4 | 5 | 6 | 5 | 4 | 3 | 2 | 1 | 26 |
| $\%$ | 3.84 | 7.69 | 11.54 | 15.38 | 19.23 | 26.09 | 19.23 | 15.38 | 11.54 | 7.69 | 3.84 | 100 |

Rolling a 7 is $26.09 \%$
Craps（2 or 12 ）is $7.69 \%$ ，the SUM of $2 \%$ and $12 \%(3.84+3.84)$ ．
For independent events，$A$ and $B$ is the product $P_{A} X P_{B}$ ，while $A$ or $B$ is the sum $P_{A}+P_{B}$

## When is a finesse like a coin flip?

- When we lack INFORMATION!!! (a priori)
- 2 Cases: Win or lose finesse
- Just like coin: Heads or Tails
- Therefore Finesse is 50\%, lacking other information


## Bridge Hands - BIG NUMBERS

- 635,013,559,600 - \# of ways to deal 13 cards.
- 53,644,737,765,488,792,839,237,440,000 the number of possible ways to deal all 52 cards, 13 at a time.
- Odds of 4 players being dealt all 13 cards in one suit:

1 in 2,235,197,406,895,366,368,301,559,999

## Which Hand is More Likely?

- AKQJ1098765432
- AK32
- K984
- Q10
\& J107


## The Trap?

What I gave
¢ AK32

- K984

Q10
\$ J107

What you saw: What you assumed:

## - AKxx

- Kxxx

Q10
\$ J10x


## SUIT SPLITS

- \# of specific cases / \# Total Cases (approximately)
- \# Total Cases $=2^{\mathrm{m}}$ (where $\mathrm{m}=\#$ missing cards)
- Study 2-7 missing cards (4-128 Tot. Cases)

| Split |  | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 7 | 0.5 | 7 | 30.5 | 62 |
|  | 6 | 1.5 | 14.5 | 48 | 36 |
|  | 5 | 4 | 28 | 68 |  |
|  | 4 | 10 | 50 | 40 |  |
|  | 3 | 22 | 78 |  |  |
|  | 2 | 48 | 52 |  |  |

## DROP Missing Honors

|  | \% | H | Hx | Hxx | TOT |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 0.4 | 4 | 18 | 22.4 |
|  | 7 | 1 | 9 | 27 | 37 |
|  | 6 | 2.4 | 16 | 36 | 54.4 |
|  | 5 | 6 | 27 | 41 | 74 |
|  | 4 | 12 | 41 | 37 | 90 |
|  | 3 | 26 | 52 | 22 | 100 |
|  | 2 | 52 | 48 |  | 100 |

## Suit Combinations

- How to play suits - wrong when done alone right when done in the context of whole hand.
- Know \# tricks needed.
- Vacant Spaces 13 each, reduced by information.


## a priori Suit Combinations

1. K3 opposite 6710QA Do you finesse for the 10? Why/Not?
2. AJ975 -- K1086 - You play the K. LHO plays the 2 RHO the 3 . You play the 6 to dummy. LHO plays the 4. Finesse or drop?
3. AQ97 opposite K108 - You play the 10 to the Q and the 7 to the K, RHO playing 2,4. LHO playing 3,5 . Now you continue the 8 and LHO plays the 6 . Finesse or drop?
4. AJ1074 opposite $\mathbf{5 2}$ (need 3 tricks)
5. AKQ74 opposite 52 (need 4 tricks; Need 5 tricks) NO SIDE ENTRIES.

## Suit Combination 1

- K3 opposite 6710QA Do you finesse for the 10? Why/Not?
- Absent information the finesse is worth $50 \%$.
- If we are looking for the J, then we can win when the J is singleton, doubleton or Jxx in either hand.
- Combining those chances results in $2.4+16+36=54.4 \%$ so cashing tops is better.

What Information would make you change your play?

- Count of the hand $\rightarrow$ split known
- \# Tricks needed from this suit
- Avoid having DANGER HAND on lead
- Can ruff out the suit


## Suit Combination 2

- AJ975 -- 6810K - You play the K. LHO plays the 2 RHO the 3 . You play the 6 to dummy. LHO plays the 4. Finesse or drop?
- Any 2-2 break is $40 \%$ while any 3-1 break is 50\%.
$-2-2$ has 6 cases. 3-1 has 8 . So the specific case for 3-1 is less likely (absent additional information).
- The Qxx w/ LHO is 6.21\%. The Qx with RHO is 6.78\%.
- The ratio 6.78/13 = 52.2\%.
- Vacant spaces says LHO has 11 while RHO has 12 before declarer's choice. $12 / 23=52.2 \%$ the Q is with RHO.

What Information would make you change your play?

## Suit Combination 3

- AQ97 opposite 810K - You play the 10 to the Q and the 7 to the K, RHO playing 2,4. LHO playing 3, 5. Now you continue the 8 and LHO plays the 6. Finesse or drop?
- You have seen 3 insignificant cards from LHO and 2 from RHO.
- That leaves 10 spaces for LHO and 11 for RHO.
- Therefore the probability that the J is with LHO is $11 /(10+11)=52.4 \%$. DROP

What Information would make you change your play?

## Suit Combination 4

- AJ1074 opposite 52 - Goal: 3 tricks
- We are missing the KQ9863
- From the chart, 3-3 happens $36 \%$ of the time and $4-2$ happens $48 \%$ of the time.
- Missing 6 cards there are $2^{6}=64$ total cases.
- 6 cards taken 3 at a time counts to 20
- 6 cards take 2 (or four) at a time counts to 30
- Any 3-3 means we win 3 tricks. Any 1-5 or 0-6 and we fail. Ignore these.
- 4-2/2-4 is where we can gain advantage. A finesse helps only when KQ63-89 is the distribution (One Case), and Hx-Hxxx (4 Cases).
- Playing small to the A and SMALL from length works for the 8 cases where Hxxx - Hx / Hx - Hxxx plus the 2 cases KQ-9863 or 9863-KQ. 10 Cases
- Ace then small is better a priori than the $1^{\text {st }}$ round finesse.

What Information would make you change your play?

## Suit Combination 5

- AKQ74 opposite 52 (need 4 tricks; Need 5 tricks)
- Needing 5 tricks, we play top down, for a 36\% chance (3-3 split).
- Needing 4 tricks we can do better. If we duck the first trick we will get 4 tricks if the suit splits 3-3 (36\%) or 4-2/2-4 (48\%). This improves our chances to $84 \%$. Much better than playing the suit top down (remember we have no outside entry).

What Information would make you change your play?

## Suit Split Probability

Richard Pavlicek Bridge Site: http://www.rpbridge. net/

Case: Missing 6 cards including the Q

Best way to answer the question "WHY??"

Now the fun starts!

| \# | A | B | C | D | West | East | Ways | Ratio | Percent |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\square$ | $\checkmark$ | $\square$ | $\square$ | Qxxxxx | - | 1 | 24 | 0.75 |
| 2 | $\square$ | $\checkmark$ | $\square$ | $\square$ | Qxxxx | x | 5 | 195 | 6.06 |
| 3 | $\square$ | $\checkmark$ | $\square$ | $\square$ | Qxxx | xx | 10 | 520 | 16.15 |
| 4 | $\checkmark$ | $\square$ | $\checkmark$ | $\square$ | Qxx | xxx | 10 | 572 | 17.76 |
| 5 | $\checkmark$ | $\square$ | $\checkmark$ | $\checkmark$ | Qx | xxxx | 5 | 260 | 8.07 |
| 6 | $\checkmark$ | $\square$ | $\checkmark$ | $\checkmark$ | Q | xxxxx | 1 | 39 | 1.21 |
| 7 | $\square$ | $\square$ | $\checkmark$ | $\checkmark$ | xxxxx | Q | 1 | 39 | 1.21 |
| 8 | $\square$ | $\square$ | $\checkmark$ | $\nabla$ | xxxx | Qx | 5 | 260 | 8.07 |
| 9 | $\square$ | $\square$ | $\square$ | $\square$ | xxx | Qxx | 10 | 572 | 17.76 |
| 10 | $\square$ | $\square$ | $\square$ | $\square$ | xx | Qxxx | 10 | 520 | 16.15 |
| 11 | $\square$ | $\square$ | $\square$ | $\square$ | x | Qxxxx | 5 | 195 | 6.06 |
| 12 | $\square$ | $\square$ | $\square$ | $\square$ | - | Qxxxxx | 1 | 24 | 0.75 |
| Goal to win |  |  |  |  |  | Totals | 64 | 3220 | 100.00 |
| A | Q, Qx, Qxx onside |  |  |  |  | 3 | 16 | 871 | 27.05 |
| B | Ruff the 4th Club |  |  |  |  | 3 | 16 | 739 | 22.95 |
| C | Play off 3 rounds of Clubs |  |  |  |  | 6 | 32 | 1742 | 54.10 |
| D | Q drops in 2 rounds |  |  |  |  | 4 | 12 | 598 | 18.57 |

## Combining Chances

- PAJ1097 opposite 543
- What is the probability you can score 4 tricks?
- p Both $\Phi$ A\&K are onside: 24\%
- p Honors are split

52\%

- $p$ Both honors are on your right

24\%
$P$ Success $=24 \%+52 \%=76 \%$

- We Need: Finesse in Suit A, and if that fails a 3-3 break in suit B. What is the probability we make our contract?
- $50 \%$ Finesse wins + 50\% Finesse loses X (36\% 3-3 split) $=68 \%$
$-\mathbf{P}_{1 \text {-success }}+\mathbf{P}_{1 \text {-fail }}\left(\mathbf{P}_{2 \text {-Success }}\right)$
- Notice that independent plays (NOT finesses) chances ADD.
- Requiring 2 or more finesses multiplies fractions.


## Analyze $1^{\text {st }}-$ Plan $2^{\text {nd }}$

The Whole Bridge Hand

- Use ALL your information - Bidding \& Play
- Start with a flexible picture of declarer/opponent
- Count hand winners and losers ("off the top") and SLOW LOSERS
- Count entries
- Count stoppers in threat suits.
- Count HCP - Your total and their total
- Combine your chances - Source of Tricks/Trick Packets
- Avoid the DANGER HAND. Assume perfect defense.
- Modify plan as you learn - Show-outs are GOLD

Use All Information
Common Inferences

- Opening bids show 12 HCP + and 5+Cards in a Major.
- 1 NT is typically 15-17.
- Weak 2 for 7-8 HCP and 6 cards
- a 3-bid less (~6) and 6-7 cards

An INFERENCE is what we judge
INFORMATION is what we see and know. (Show outs are INFORMATION)

## Tips

## Combining Chances (Mutually Exclusive events)

- Plan for failure - Stay ALIVE.
- Find chances that create options
- Cash winners in your long side suit (drop honors)
- Finesse long suits into safe hands when necessary.
- Avoid finesses completely if possible
- Leave short suits (no extra chances) until the end.


## Steve's Tips:

- Always choose the plan with the best probability
- Find a good plan? LOOK AGAIN. FIND A BETTER ONE
- When faced with equal choices, choose the option that allows you to STAY ALIVE longest (Take more chances)
- Any Chance is better than NO Chance
- NEVER take a PRACTICE FINESSE.


## A Simple Hand?

Contract: 4甲 , Opponents pass throughout


Analysis:
Winners: 5 Losers: 3 Fast, 1 Slow
Entries: W3 and E2
Stoppers: ${ }^{2}$ 2,
Source of Tricks: \$(3), \$(2)

## Improving Your Plan

Contract 6『, no opposing bidding

- AQ
- AKJ72
- AQ
\$ J456

| N | - 98 |
| :---: | :---: |
| W E | - Q10654 |
| S | - J65 |
| Lead 3 | \& AK10 |

ANAYLSIS:
Winners: 9 Losers: 0 Fast, 3 Slow
Entries: W5 and E3
Stoppers: 14 1 2\&
Source of Tricks: (3); (2)
Plan 6

## Improving your plan 1

- AQ
- AKJ72
- AQ
\$ J 456

| N | ¢ 98 |
| :---: | :---: |
| W E | - Q10654 |
| S | - J65 |
| Lead ${ }^{\text {P }}$ | \$ AK10 |

A Novice (or finesse-aholic)

- sees 3 finesses, draw trumps in 2-4 rounds and begin.
- 3 Finesses here are independent (different suits, different players) so the odds of all 3 are $1 / 2 \times 1 / 2 \times 1 / 2$ or 12.5 \%.
- They need only 2 of the 3 finesses. How do you calculate the probability? Think: 2 winning finesses is the same case as one losing finesse or $\mathbf{5 0 \%}$.


## Improving your plan 2



## Intermediate Player:

- After pulling trumps if the finesse works and they split 3-3, they can pitch a losing on the long $\$$
Combining chances that way means:
- $50 \%$ finesse $\times 36 \% 3-3$ - split $=18 \%$
- $50 \%$ Finesse x $82 \%$ remaining $=41 \%$ or
- TOTAL CHANCE:

59\%
a useful improvement.

## Improving your plan 3

## - AQ <br> - AKJ72 <br> - AQ <br> \& J456

Expert Player:

- Cash the AK
- \% Time North has 0, 1, 2 \&
- Finesse ( $50 \% \times 56 \%$ )
- TOTAL

$$
\begin{aligned}
& =18 \%+ \\
& =26 \% \quad(\text { NOT Q, Qx) } \\
& =28 \% \\
& 72+\%
\end{aligned}
$$

- Look deeper! Treat the hand as "one of 2 finesses": Finesse $\$$. If win, cash tops. If no $\$$, finesse away on $3^{\text {rd }} \downarrow$. Likewise if $\$$ finesse loses, we need only the finesse to win (Pitch the losing on the $\boldsymbol{\$}$ ) - a $75 \%$ play.


## Bonus Problem

69, No opposition bids. What is the likelihood of success? Trumps split 2-1


Which finesse do you take first? Second? Why?

> ANSWER: Take NO Finesses. Draw 2 rounds of Trump and 2 rounds of $\bullet$. Then play off AKJ in that order. No matter who wins they have to either give you a free finesse or a ruff sluff - either way we lose only 1 trick.

> PROBABILITY OF SUCCESS: 100\%

## See the Ending...



Either $\mathbf{N}$ or $\mathbf{S}$ must lead and give us the rest of the tricks. You play like an expert!
ANSWER: Take NO Finesses. Draw 3 rounds of Trump and 2 rounds of $\bullet$. Then play off AKJ in that order. No matter who wins they have to either give you a free $\$$ finesse or a ruff sluff - either way we lose only 1 trick.

## PROBABILITY OF SUCCESS: 100\%

## Other Uses for "p"

- When to bid Game, Small Slam, and Grand Slam
- The likelihood of success must match or exceed breakeven
- Breakeven - what you win equals what you lose.


## Game, Slam \& Grand Odds

|  | Games |  | Small Slam |  | Grand Slam |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Type | V | NV | V | NV | V | NV | V | NV |
| Score+ | 620 | 420 | 1430 | 980 | 2210 | 1510 | 2210 | 1510 |
| Score- | -100 | -50 | -100 | -50 | -100 | -50 | -100 | -50 |
| Not Bid | 170 | 170 | 680 | 480 | 1460 | 1010 | 710 | 510 |
| Win | +450 | +250 | 750 | 500 | 750 | 500 | 1500 | 1000 |
| Lose | -240 | -190 | 750 | 500 | 1530 | 1030 | -780 | -530 |
| IMPs W | 10 | 6 | 13 | 11 | 13 | 11 | 17 | 14 |
| IMPs L | -6 | -5 | -13 | -11 | -17 | -14 | -13 | -11 |
| Break <br> Even | $38 \%$ | $45 \%$ | $50 \%$ | $50 \%$ | $57 \%$ | $56 \%$ | $43 \%^{*}$ | $44 \%^{*}$ |

*If opponents bid game, then bidding a Grand Slam is Poor. With 12 tricks, a slam gains $+11 \mathrm{NV} \&+13 \mathrm{~V}$ IMPS, the grand loses -11NV Imps and -13V, swinging -22NV \& -26V Imps. Avoid grand slams when they only bid game. Need 14 tricks.

## Useful a priori \%:

- Have FUN playing BRIDGE $\frac{\%}{100}$
- Need 1 of 2 finesses (same hand) 76
- Missing cards split 3-2 68
- Missing cards split 4-3 62
- Q drops in 3 rounds when holding 7 cards 54.4
- Pure finesse 50
- Need 2 finesses of 3 available 50
- Q drops in 3 rounds when holding 6 cards 37
- Suit splits 3-3 36
- Need 3 finesses of 4 available. 31
- Need 2 finesse of 2 available 25
- Need finesse \& 3-3 split 18
- Need 3 finesses 12.5


## References

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See you at the tables!

## THANK YOU FOR YOUR KIND ATTENTION!

